FIRST SEMESTER (CBCSS—UG) DEGREE EXAMINATION, NOVEMBER 2021

B.C.A.

BCA 1C 02—DISCRETE MATHEMATICS

(2021 Admissions)

Time: Two Hours

Maximum: 60 Marks

Section A (Short Answer Type Questions)

Answer at least **eight** questions.

Each question carries 3 marks.

All questions can be attended.

Overall Ceiling 24.

- 1. Define contradiction.
- 2. Define dual of proposition. Write the dual of $(P \land Q) \lor T$
- 3. Show that $\neg P \land P$ is a tautology.
- 4. Explain universal quantifier.
- 5. Define transitive relation. Show whether the relation $R = \{<1, 2>, <2, 3>, <1, 3>, <2, 1>\}$ is transitive.
- 6. Define Boolean algebra.
- 7. Define minterm.
- 8. Define partially ordered set.
- 9. Define subgraph of a graph with an example.
- 10. Define Euler Graph.
- 11. Define isolated vertex of a graph. Give an example.
- 12. Define an m-ary tree.

 $(8 \times 3 = 24 \text{ marks})$

Section B (Short Answer Essay Questions)

Answer at least **five** questions. Each question carries 5 marks. All questions can be attended. Overall Ceiling 25.

- 13. Prove distributive law in logic using truth table.
- 14. Show that $P \longrightarrow (Q \longrightarrow R) \Leftrightarrow (P \land Q) \longrightarrow R$ using laws of logic.

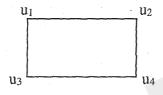
Turn over

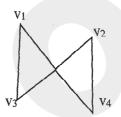
D 12609

- 15. Let $X = \{1, 2, 3, 4\}$ If $R = \{\langle x, y \rangle / x \rangle y, x \& y \in X\}$.
 - (a) Write the elements of R and its matrix.
 - (b) Draw the digraph represents the relation.
- 16. Define equivalence class. Also write the equivalence classes modulo 3 generated by the elements of Z.

2

- 17. Show that the $\langle P(X), \subseteq \rangle$ is a partially ordered set, where X is any set and P(X) is the power set of A.
- 18. Define isomorphism between two graphs. Show that the following graphs are isomorphic.





19. Show that in a complete binary tree the total number of edges is given by $2(n_i - 1)$. Where n_i is the number of terminal nodes.

 $(5 \times 5 = 25 \text{ marks})$

Section C (Essay Type Questions)

Answer any **one** question. The question carries 11 marks.

- 20. Explain relation on a set. Also explain different types of relation on a set. Give examples for each relation.
- 21. (a) Explain Travelling Salesman Problem.
 - (b) Explain Breadth-first search algorithm for spanning tree.

 $(1 \times 11 = 11 \text{ marks})$