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FIRST SEMESTER (CBCSS—UG) DEGREE EXAMINATION NOVEMBER 2021

Mathematics

MTS 1C 01-MATHEMATICS-I

(2021 Admissions)

Time : Two Hours

Maximum : 60 Marks

Section A

Answer at least **eight** questions. Each question carries 3 marks. All questions can be attended. Overall Ceiling 24.

- 1. Calculate the slope of the tangent line to the graph of $f(x) = x^2 + 1$ when x = -1.
- 2. Find $\lim_{x \to 1} \frac{x^2 + x 2}{x^2 x}$.
- 3. Find the derivative of $y = \sqrt{x}$ for x > 0.
- 4. Find $\frac{d}{dx} \Big[\cos \left(\sqrt{1 + \cos x} \right) \Big]$.
- 5. Find the linearization of $f(x) = \cos x$ at $x = \pi/2$.
- 6. Show that there is a number *c* such that $c^3 c^2 = 10$.
- 7. Find $\lim_{t \to 0} \cos\left(\frac{x}{\sqrt{19 3 \sec 2t}}\right)$.
- 8. Suppose that f is differentiable on the whole real line and that f'(x) is constant. Prove that f is linear.

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- 9. Find the critical points of $f(x) = 3x^4 8x^3 + 6x^2 1$.
- 10. Find the inflection points of $f(x) = x^2 + (1/x)$.
- 11. Using limits of Riemann sums, establish the equation $\int_{a}^{b} c \, dx = c \, (b a)$, where c is a constant.

12. Find
$$\int_0^2 \left(\frac{t^2}{4} - 7t + 5\right) dt$$
.

 $(8 \times 3 = 24 \text{ marks})$

Section **B**

Answer at least **five** questions. Each question carries 5 marks. All questions can be attended. Overall Ceiling 25.

13. Find
$$\lim_{h \to 0} \frac{\sqrt{2+h} - \sqrt{2}}{h}$$

14. Show that the line y = mx + b is its own tangent at any point (x, mx + b) on the line.

- 15. Assume that oil spilled from a ruptured tanker spreads in a circular pattern whose radius increases at a constant rate of 1 ft/s. How fast is the area of the spill increasing when the radius of the spill is 20 ft ?
- 16. Use implicit differentiation to find d^2y/dx^2 if $5x^3 7y^2 = 10$.
- 17. Find the maximum and minimum points and values for the function $f(x) = (x^2 8x + 12)^4$ on the

interval [-10, 10].

18. Use l'Hôpital's Rule to find $\lim_{x \to 0} \frac{\sin x - x}{x^3}$.

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19. Find the area of the region between the *x*-axis and the graph of $f(x) = x^3 - x^2 - 2x, -1 \le x \le 2$.

 $(5 \times 5 = 25 \text{ marks})$

Section C

Answer any **one** question. The question carries 11 marks.

20. (a) Find the area of the region in the first quadrant that is bounded above by $y = \sqrt{x}$ and below by the *x*-axis and the line y = x - 2.

(b) Find
$$\frac{dy}{dx}$$
 if $y = \int_{1}^{x^2} \cos t \, dt$.

- 21. (a) Find the absolute extrema of $h(x) = x^{2/3}$ on [-2, 3].
 - (b) Find the volume of the solid generated by the revolution about the x-axis of the loop of the

curve
$$y^2 = x^2 \frac{3a-x}{a+x}$$
.

(c) Evaluate
$$\lim_{x \to 0} \left(\frac{1}{x^2} - \frac{1}{\sin^2 x} \right)$$

 $(1 \times 11 = 11 \text{ marks})$